Tunable Anisotropy in Inverse Opals and Emerging Optical Properties

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ABSTRACT: Using self-assembly, nanoscale materials can be fabricated from the bottom up. Opals and inverse opals are examples of self-assembled nanomaterials made from crystallizing colloidal particles. As self-assembly requires a high level of control, it is challenging to use building blocks with anisotropic geometry to form complex opals, which limits the possible structures. Typically, spherical colloids are employed as building blocks, leading to symmetric, isotropic superstructures. However, a significantly richer palette of directionally dependent properties are expected if less symmetric, anisotropic structures can be created, especially originating from the assembly of regular, spherical particles. Here we show a simple method for introducing anisotropy into inverse opals by subjecting them to a post-assembly thermal treatment that results in directional shrinkage of the silica matrix caused by condensation of partially hydrated sol–gel silica structures. In this way, we can tailor the shape of the pores, and the anisotropy of the final inverse opal preserves the order and uniformity of the self-assembled structure. Further, we prevent the need to synthesize complex oval-shaped particles and crystallize them into such target geometries. Detailed X-ray photoelectron spectroscopy and infrared spectroscopy studies clearly identify increasing degrees of sol–gel condensation in confinement as a mechanism for the structure change. A computer simulation of structure changes resulting from the condensation-induced shrinkage further confirmed this mechanism. As an example of property changes induced by the introduction of anisotropy, we characterized the optical spectra of the anisotropic inverse opals and found that the optical properties can be controlled in a precise way using calcination temperature.

INTRODUCTION

Self-assembly provides a way to structure materials with nanoscale dimensions without using expensive, complicated, and time-consuming top-down fabrication methods. However, self-assembly requires a high level of control over the assembly conditions and the morphology and composition of individual unit elements. This limits the choice of constituent building blocks that can be used and hence the variety of accessible assembly structures formed by the building blocks’ minimum-free-energy arrangements. In particular, spherical colloids form highly symmetric, face-centered cubic crystals, called opals. This structure can be inverted to form an inverse opal by filling in the interstitial spaces and removing the colloidal template, resulting in a continuous matrix of periodically arranged, interconnected voids with the same symmetry as the original colloidal template.

Inverse opals with high long-range order can be made using a co-assembly process. A thin film is grown by evaporative deposition of polymeric colloids in the presence of a silica sol–gel precursor that condenses in the colloidal crystal interstitial spaces. The co-assembly method allows the growth of extremely highly ordered crystals with single domains stretching over macroscopic dimensions. Upon calcination, the polymeric colloids are completely combusted and the silica precursor fuses into a dense silicon dioxide scaffold, creating a hexagonal close-packed array of interconnected voids.

Highly interconnected porosity and long-range order are two key attributes of inverse opal structures that make them valuable for a variety of applications. Because of their periodic nature, inverse opals are a versatile material platform for controlling electromagnetic and acoustic wave propagation. In particular, if their periodicity is tailored to the length scale of the wavelength of visible light, inverse opals interact strongly with visible light, allowing applications in solar cells, as light-emitting diodes, and as structural color-based coatings. In addition, inverse opals’ interconnected...
porosity and high surface area are essential for their use in many other contexts, including batteries and catalysts, as well as sensors of liquid media, scaffolds for tissue engineering, substrates for omniphobic surfaces, and materials for studying diffusion processes in confinement. All of these remarkable properties of inverse opals depend strongly on the precise control over the structural uniformity. Spherical colloids are simple to synthesize and crystallize, so they are typically used as templates. However, anisotropic structures would offer a range of unique, direction-dependent properties because of the changes in the angular periodicities and directional porosity and are therefore highly desirable, but a simple method for obtaining anisotropic inverse opals is necessary to investigate these directional properties.

Prior research efforts to form ordered structures with different morphologies have primarily focused on the design and crystallization of anisotropically shaped colloidal particles. However, their synthesis is demanding, and crystallization into uniform, defect-free structures remains a challenge. Successful examples include crystallization of gold nanorods, assembly of anisotropic magnetic particles in magnetic fields, DNA templating of anisotropic colloidal crystals, and, more recently, assembly of anisotropic silica rods in an electric field. These anisotropic structures have important directional properties and have been used for plasmonic sensing. Alternatively, the challenges of synthesizing and crystallizing anisotropic particles can be avoided by introducing anisotropy after the assembly of isotropic building blocks, for example, by mechanical deformation of elastomeric inverse opal structures.

Here we describe a simple approach to creating anisotropy in inverse opal structures consisting of an inorganic, nonflexible metal oxide matrix. Our approach allows us to precisely tailor the anisotropy while preventing the need for complex crystallization techniques. Instead, we take advantage of the molecular state of the structure to introduce anisotropy. Silica sol–gel materials undergo condensation of the remaining hydroxyl groups at high temperatures, leading to a decrease in volume via loss of water. In the co-assembly process, the material is deposited on a substrate that holds the sol–gel material in place. This surface constraint prevents shrinking in the plane of the substrate and leads to directional out-of-plane contraction of the film, as shown schematically in cross section in Scheme 1. This provides a facile method for introducing anisotropy into the system after assembly, resulting in controlled changes in the inverse opal properties. We present a detailed investigation of this calcination-induced anisotropy in self-assembled inverse opals. The calcination temperature controls the degree of condensation, as confirmed using X-ray photoelectron spectroscopy (XPS) and infrared spectroscopy (IR). The amount of shrinkage directly relates to the degree of condensation, allowing us to precisely alter the pore shape and to tailor properties that depend strongly on the pore geometry of the structure. In particular, we demonstrate how the optical properties of inverse opals change with an increase in anisotropy. It is important to note that the anisotropy is generated during post-assembly processing, thus circumventing the complex synthesis and assembly of anisotropic building blocks. Instead, a generalized and reliable assembly strategy of spherical particles is used to generate crystals with an adjustable pore shape anisotropy.

**EXPERIMENTAL SECTION**

**Chemicals and Materials.** Inverse opals were synthesized using a process described in detail elsewhere. Briefly, polystyrene colloids with diameters of 230, 330, and 410 nm were synthesized using a surfactant-free emulsion polymerization process. They were then diluted in water, yielding a 0.1% solid content in a total volume of 20 mL; 150 μL of a prehydrolyzed tetraethyl orthosilicate (TEOS) solution (1:1:1.5 TEOS:0.1 M HCl:ethanol by weight, stirred for 1 h) was added, and the mixture was sonicated. A silicon wafer was suspended vertically in the vial. The vial was then placed inside an oven for 2 days to allow for evaporation of the solvent, leaving behind a colloidal crystal with a silica matrix surrounding it. A Memmert UF110 oven set to 65 °C stabilized by a pneumatic vibration-free table was used for the co-assembly process. The colloidal crystal template was removed by submersion in either toluene or tetrahydrofuran overnight to dissolve the polystyrene or by calcination to 500, 600, 800, 1000, or 1100 °C using a heating and cooling rate of 2 °C/min and a 2 h hold, except for the case of 1100 °C, which was held at the final temperature for an extended period of 5 h. A Lindberg Blue M box furnace from Thermo Scientific was used for calcination. Calcination temperatures below 500 °C were not used to ensure complete removal of the polystyrene template. Deionized water was used from a Milli-Q system; ethanol was obtained from Koptec, and all other reagents (0.1 M HCl, styrene, and tetraethyl orthosilicate) were obtained from Sigma-Aldrich.

**Sample Characterization.** Scanning electron microscopy (SEM) was performed using a Zeiss Ultra Plus field emission scanning electron microscope. ImageJ was used for subsequent image analysis, including the width:height ratio calculations, based on the pixel size from the Zeiss SEM software.

X-ray photoelectron spectroscopy (XPS) was performed using a Thermo Scientific K-Alpha XPS system. Low resolution survey scans were taken followed by high resolution scans with a dwell time of 50 ms and a resolution of 0.1 eV for the individual elements, with 10 scans averaged. The high resolution Si 2p and O 1s scans were used for quantification. Attenuated total reflectance (ATR) infrared (IR) spectroscopy was performed using a Bruker Vertex 70 FTIR spectrometer equipped with a MIRacle attenuated total reflectance accessory. For each spot, 128 scans were averaged over the range of 600–4000 cm⁻¹ at 4 cm⁻¹ resolution.

For the optical measurements taken at normal incidence, a Leica DM2500 microscope was used with an Ocean Optics USB2000+ spectrometer. A 96% reflective mirror was used as a reference. Measurements of reference and sample spectra were performed under identical configurations; thus, the data are displayed as absolute intensity. For the variable-angle spectrometry studies, an Ocean Optics DH-2000 UV–vis–NIR light source was used to illuminate a small
anisotropic inverse opals were made using a slight modification of the synthesis procedure. The co-assembly of inverse opals involves one crystal growth step, in which a substrate (usually a silicon wafer) is submerged in a dispersion of polymeric colloids and prehydrolyzed tetraethyl orthosilicate (TEOS) in water. The water is evaporated at 65 °C, forming a thin polymer/silica film on the substrate. Next, the sample is calcined at 500 °C to combust the colloids and sinter the sol–gel silica, leaving behind an ordered, porous silica structure. Changing this final calcination step results in an altered pore structure (Figure 1), giving access to different pore geometries. With spherical pore symmetry arising from the shape and size of the colloids, the as-grown structure can be obtained by dissolving the colloids with toluene or tetrahydrofuran (Figure 1A, left). By increasing the calcination temperature, we obtained different degrees of anisotropy of the structure, with increasingly deformed pores (Figure 1A). Growing the matrix and template in a single, one-pot synthesis allows for large (centimeter-scale) domains, and this high degree of order is retained even at high calcination temperatures (Figure S1 of the Supporting Information). Changing this boundary condition was applied on a unit cell in the lateral direction. A linear elastic material model was used. The shrinkage of the material was simulated as thermal strain. The displacement and rotation of the inverse opal structure proximate to the substrate were constrained, and a periodic boundary condition was applied on a unit cell in the lateral direction. The ratio of pore width to pore height was recorded as a function of the linear shrinkage.

![Figure 1](image1.png)

Figure 1. (A) Cross-sectional scanning electron microscope images of samples made with 230, 330, and 410 nm polymer colloids as templates. Different samples are shown after template removal by solvent dissolution at room temperature (left) and by calcination at 500, 800, and 1100 °C (from left to right). All scale bars are 400 nm. (B) Quantification of the anisotropy as a function of calcination temperature. The ratio of pore width (w) to pore height (h) for all samples was measured from the SEM images (~25 measurements per sample). Error bars represent the standard deviation of these measurements assuming a Gaussian distribution.

■ RESULTS AND DISCUSSION

Anisotropic inverse opals were made using a slight modification of the synthesis procedure. The co-assembly of inverse opals involves one crystal growth step, in which a substrate (usually a silicon wafer) is submerged in a dispersion of polymeric colloids and prehydrolyzed tetraethyl orthosilicate (TEOS) in water. The water is evaporated at 65 °C, forming a thin polymer/silica film on the substrate. Next, the sample is calcined at 500 °C to combust the colloids and sinter the sol–gel silica, leaving behind an ordered, porous silica structure. Changing this final calcination step results in an altered pore structure (Figure 1), giving access to different pore geometries. With spherical pore symmetry arising from the shape and size of the colloids, the as-grown structure can be obtained by dissolving the colloids with toluene or tetrahydrofuran (Figure 1A, left). By increasing the calcination temperature, we obtained different degrees of anisotropy of the structure, with increasingly deformed pores (Figure 1A). Growing the matrix and template in a single, one-pot synthesis allows for large (centimeter-scale) domains, and this high degree of order is retained even at high calcination temperatures (Figure S1 of the Supporting Information). Using the ratio of pore width to pore height to quantify the variation in the geometry, we see that the anisotropy introduced into the structure as a function of calcination temperature follows a roughly linear trend with temperature (Figure 1B). In all cases, the same heating rate (2 °C/min) was used, and the final temperature was held for 2 h, except for the case of 1100 °C, which was held for an extended period of 5 h.

**Chemical Analysis of Si–OH Condensation.** To determine what causes the observed structural changes on a molecular level, we used XPS and ATR-IR spectroscopy (Figure 2). XPS provides nanoscale surface-sensitive elemental information, whereas ATR-IR provides information about the chemical environment and probes farther into the structure. Together, the results allow us to probe the level of condensation at different calcination temperatures.

XPS confirms that silicon and oxygen are the only elements present in our silica film (Figure 2A). Further, the ratio of these...
two elements provides a way to monitor the condensation of the sol–gel silica: the Si:O ratio increases when two residual Si–OH groups cross-link to form Si–O–Si and release a water molecule (Scheme 1). As shown in Figure 2B, we see an increase in the Si:O ratio with higher calcination temperatures, indicating that additional condensation is occurring. The ratio begins to level out at the value for a reference silica layer (horizontal dotted line) around 1000 °C.

This analysis is further confirmed with the ATR-IR spectra shown in Figure 2C. The peak at 970 cm⁻¹, characteristic of the Si–OH vibration, is shown in the inset. To better compare the peaks, the peak area at 970 cm⁻¹ for each temperature is normalized by the peak area of the antisymmetric Si–O–Si vibration at 1070 cm⁻¹ and shown in Figure 2D. The Si–OH peak disappears at the higher calcination temperatures, indicating that Si–OH bonds are no longer present and further confirming that condensation is occurring.

**Shrinking of Inverse Opal Films.** Condensation of silica sol–gel materials is known to cause shrinkage of the resulting silica. Because the silica inverse opals are confined in the lateral plane by the attachment to the silicon wafer substrate, a decrease in the volume of the solid phase upon condensation causes shrinkage only in the direction perpendicular to the substrate (Figure 3A). To confirm that the substrate is preventing the matrix from shrinking in the lateral directions, we decoupled the inverse opal film from the substrate upon calcination using a thin layer of photoresist as a sacrificial layer deposited prior to the growth step. After assembly, this inverse opal film on a photoresist layer underwent calcination as before, and the sacrificial layer disintegrated with the colloids, causing the film to separate from the substrate (Figure 3B).

While films bound to a substrate show anisotropic pores (Figure 3C), the pores from samples with a sacrificial layer appeared to be isotropic (Figure 3D). The anisotropy ratios of the pores from the bound films match those in Figure 1B, but the pores in the released films are the same size in both measured dimensions (Table 1). As determined by comparison of the 500 °C sample and 1100 °C samples in Table 1, the pores shrink ~18% in each direction without a confining substrate; however, the width stays the same but the height shrinks ~42% for the substrate-bound sample. The pores of the unbound films shrink less in the vertical direction (18% vs 42%), but they shrink in all directions equally; on the other hand, all of the condensation-induced volume loss must be accommodated by the perpendicular direction on the substrate-bound films. In both cases, this corresponds to a ~40–45% volume loss, similar to what is seen in silica sol–gel films.

The effect of the substrate is also visible in samples with cracks. When cracks occasionally form in inverse opals, the top layers become less confined along the substrate. The cracks can provide stress release sites in films annealed to high temperatures. Thus, while the bottom layers still deform perpendicularly to the substrate, the top layers can now shrink more isotropically (Figure 4), creating a difference in pore dimensions between the upper and lower layers.

![Figure 3. Effect of the substrate on pore anisotropy during calcination.](image)

![Figure 4. SEM image of a crack in an inverse opal made from a 230 nm colloidal template annealed to 800 °C.](image)

| Table 1. Comparison of Inverse Opal Pores with and without a Substrate |
|---------------------------|--------|--------|------|
| calcination temperature   | w (nm) | h (nm) | wh  |
| 500 °C (substrate)        | 320 ± 14 | 240 ± 16 | 1.33 |
| 1100 °C (substrate)       | 330 ± 14 | 140 ± 19  | 2.36 |
| 500 °C (extra layer)      | 330 ± 15 | 340 ± 14  | 0.97 |
| 1100 °C (extra layer)     | 280 ± 23 | 270 ± 17  | 1.04 |

The formation of the anisotropic structure is due to the shrinkage of the material while it is constrained on the bottom, so we expect a dependence on thickness. One way that this manifests itself is in edge effects. The size of the region influenced by the edge is comparable with the thickness of the film. In the middle part of the sample far from the edges, the film is under homogeneous deformation. As long as the lateral dimension of the sample is much larger than its thickness, there is always a region in the middle part of the sample where uniform opal structures are formed. Because the films were prepared over macroscopic dimensions, we expect a high...
degree of homogeneity with little influence of sample edges. Previous studies found that cracks naturally form in co-assembled inverse opals once the film exceeds a thickness of approximately 20 colloid layers. As shown in Figure 4, such cracks prevent consistent anisotropic pore shrinkage and thus compromise the quality of the anisotropic film. Fortunately, large areas without cracks are possible with the co-assembly method. As long as the crack formation threshold is approximately 20 colloid layers. As shown in Figure 4, such cracks prevent consistent anisotropic pore shrinkage and thus compromise the quality of the anisotropic film. Fortunately, large areas without cracks are possible with the co-assembly method. As long as the crack formation threshold is

<table>
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<th>calcination temperature</th>
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<tr>
<td></td>
<td>w (nm)</td>
<td>h (nm)</td>
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<tr>
<td>65 °C (as synthesized)</td>
<td>370 ± 16</td>
<td>330 ± 17</td>
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<tr>
<td>800 °C</td>
<td>420 ± 33</td>
<td>270 ± 15</td>
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<tr>
<td>1100 °C</td>
<td>370 ± 13</td>
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The simulation and experimental results were compared using the ratio of pore width to pore height (Table 2). Specific values of the simulation (3, 10, and 22% shrinkage) were chosen to match the pore w:h ratio to experimental examples (1.12, 1.5, and 2). Thus, we were able to correlate the experimental calcination temperature with the amount of contraction that caused the geometry shown in the simulation. Assuming both horizontal directions are equivalent in the three-dimensional experimental case, this gives an estimate that the silica matrix shrinks 40% in volume upon calcination at 1100 °C. This agrees with the one- and three-dimensional contraction values we see, as well as with previous results measuring shrinkage of silica sol–gel materials.

Optical Properties of Anisotropic Inverse Opals. The diameter of the templating colloidal particles was chosen to be several hundred nanometers, giving the inverse opals a periodic structure on the scale of the wavelength of visible light; thus, they form strongly colored photonic crystals. The perceived color of the films depends on several factors, including the number of layers in the inverse opal, the refractive index contrast between the pore and matrix material, and, most importantly, the period of the repeating structure. Following Bragg’s law, the layer spacing and the peak wavelength are directly proportional. The size of the colloidal building blocks and the calcination temperature (via the amount of shrinkage) control this spacing. To minimize errors due to intersample variability, measurements of variations in the optical properties of inverse opal films as a function of preparation conditions were performed at the same spot on a single sample. The colloids were removed with a solvent before the reflectivity was measured. The film then underwent calcination to subsequently higher temperatures, yielding an optical spectrum after each heating step (Figure 5A). This experimental protocol differs slightly from that used to obtain the samples from which previous results presented in this paper were deduced. However, similar pore anisotropies develop following this sequential protocol, and they are comparable to the anisotropies described above (Figure S2 of the Supporting Information). We used 410 nm colloids as the colloidal template to ensure localization of the reflection peak across a range within the visible spectrum.

The degree of anisotropy affects the periodicity and thus the wavelengths of Bragg resonance of light within the inverse opal structure. Consequently, annealing the same inverse opal sample to subsequently higher temperatures results in an incremental blue shift of the reflection peak (Figure 5A), originating from the decrease in period along the perpendicular direction. The shift in peak wavelength varied nearly linearly (R² = 0.95) with anisotropy (Figure 5B), as expected from Bragg’s law. The small deviation from linearity can be attributed to an expected increase in the refractive index from calcination, which would produce a red shift in the spectrum at higher temperatures. The peak intensity decreased slightly at elevated calcination temperatures, perhaps because higher temperatures contribute to cracks having a change in periodicity from the top layer to the bottom layer of the crystal, as shown in Figure 4. This leads to nonuniformity in pore geometry and thus layer thickness, resulting in peak broadening and a lower reflection intensity.
The angular dependence of the optical spectra was also studied. Because the anisotropic shape of the inverse opal pores introduces a different periodicity as a function of incident angle, the angular dependence of the optical spectrum also changes when anisotropy is introduced. We obtained angularly resolved reflectance spectra to further probe the change in structure (Figure 5C). Specular reflectance spectra were obtained at incident angles from $-75^\circ$ to $75^\circ$ in $0.5^\circ$ increments with an angular resolution of $<1^\circ$. These optical spectra were then plotted against the light incidence angle to give the graphs shown in Figure 5C, where the gray scale encoded (black for high and white for low) reflection intensity is displayed as a function of light incidence angle and wavelength. The spectra qualitatively agree with other spectra in the literature, such as Guldin et al.\textsuperscript{55} or the supplementary of Hatton et al.\textsuperscript{11}. In addition, contrary to earlier reported spectra, thin-film interference-based side-band intensity undulations are resolved in the presented data due to the high angular resolution of the variable angle spectrometer.

Different crystal planes present in the structure cause reflections at different angles. When they are not parallel to the substrate plane, they lead to dips in the angular spectra that appear as diagonal white lines (red box in Figure 5C). The presence of these dips indicates that the other crystal planes are still ordered enough to reflect light by constructive interference, indicating that a high degree of order remains in the samples, even those annealed to $1100^\circ$C.

To further probe the angular dependence, we compared inverse opals with the same normal reflection peak with two different degrees of anisotropy (Figure 6). In one sample, 410 nm colloids were used for the template and calcination to $1000^\circ$C created anisotropy in the structure (Figure 6A). The periodicity of the anisotropic structure gave a normal reflection peak around $510\text{ nm}$ (lateral dashed line). A structure with a similar periodicity will produce a similar wavelength of peak around $510\text{ nm}$ (lateral dashed line). A structure with a similar periodicity will produce a similar wavelength of peak around $510\text{ nm}$ (lateral dashed line). A structure with a similar periodicity will produce a similar wavelength of peak around $510\text{ nm}$ (lateral dashed line). A structure with a similar periodicity will produce a similar wavelength of peak around $510\text{ nm}$ (lateral dashed line).

CONCLUSIONS

Anisotropic colloidal crystals have generated much interest recently. Here, we provide a method for controllably adjusting the anisotropy present in an inorganic inverse opal matrix and describe the mechanism of formation. Controlling the shape of the pores by varying the calcination temperature gives us control over the order and porosity of the resulting film and introduces anisotropic pore shapes that cannot be easily achieved by direct assembly of anisotropic particles. On the basis of XPS and IR results, as well as a finite element simulation, we propose that matrix shrinkage from sol–gel condensation is causing this change in geometry. The decreased height of the pores leads to a blue shift in the optical spectrum at higher calcination temperatures, as expected for the smaller interlayer spacing. A complete angular characterization of the optical spectra shows that three-dimensional order in the crystal is retained even with a high degree of anisotropy.

Calcination temperature can control the shape and anisotropy of inverse opal pores, allowing wide ranges of anisotropy perpendicular to the surface to be generated. In addition to the controlled tuning of the optical properties of inverse opals described here, we expect anisotropy to affect other properties, as well, such as the mechanical stability or wetting characteristics. This simple yet precise method for the control of anisotropy in three-dimensional periodic microstructures allows inverse opals to be a versatile platform for fundamental studies probing tailored confinement and structure-property relationships.

ASSOCIATED CONTENT

Supporting Information

Videos of structural simulation, volume loss calculations, and SEM cross sections of samples after optics experiments. This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

The authors declare no competing financial interest.

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